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Attorney Docket No. C00-057 First Inventor or Application Identifier UTILITY William Silver PATENT APPLICATION METHOD AND APPARATUS FOR LOCATING OBJECTS USING ...

	TRANSMITTAL	Title	UNIVERSAL ALI	IGNMENT TARGETS			<u>0</u> 5
(Only for new nong	provisional applications under 37 CFR	.53(b)) Express Ma	il Label No.	EM 067 610 794	US		>6
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See MPEP chapter 600 concerning utility patent application contents. 1. X Fee Transmittal Form (Submit an original, and a duplicate for fee processing) 2. X Specification [Total Pages 36] (preferred arrangement set forth below) - Descriptive title of the Invention - Cross References to Related Applications - Statement Regarding Fed sponsored R&D - Reference to Microfiche Appendix - Background of the Invention - Brief Summary of the Invention - Brief Description of the Drawings (if filed) - Detailed Description - Claim(s)				Washingt the Computer Program (A ide and/or Amino Acid S Computer Readable C Paper Copy (identical Statement verifying identical APANYING APPL tent Papers (cover sheet and assignee) Translation Document (ation Disclosure tent (IDS)/PTO-1449 inary Amendment the Receipt Postcard (MPE id be specifically itemize Entity	Appendix) Sequence Sopy to compute to comput	Submission (if appleter copy) above copies DN PARTS nt(s))	plicable)
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IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

In re Application of: William Silver

For: METHOD AND APPARATUS FOR LOCATING OBJECTS USING UNIVERSAL ALIGNMENT TARGETS

Attorney Docket Number: C00-057

Assistant Commissioner for Patents Box Patent Application Washington, DC 20231

NEW APPLICATION TRANSMITTAL

Dear Sir:

Transmitted herewith for filing is the patent application of William Silver, for METHOD AND APPARATUS FOR LOCATING OBJECTS USING UNIVERSAL ALIGNMENT TARGETS.

EXPRESS MAIL CERTIFICATE
Express Mail Label Number EM 067 610 794 US. Date of Deposit: /o/30/43. I hereby
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Postal Service "Express Mail Post Office to Addressee" Service under 37 CFR 1.10 on the date indicated
above, and is addressed to the Assistant Commissioner for Patents, Box Patent Application, Washington,
DG 20021
DC 20231.
,

1. Papers Enclosed That Are Required for Filing Date under 37 CFR 1.53(b)

- 36 pages of specification (including pages of claims and page of abstract)
- 8 sheets of drawings (informal)
- 18 pages of Appendix

2. Fee Calculation (37 CFR 1.16)

Item	Citation	Calculation	Am	ount
Basic filing fee	1.16(a)		\$ '	710.00
Additional claim fees:				
Independent claims	1.16(b)	(1 indep. claims - 3) x 80.00	\$.00
Total claims in excess of 20	1.16(c)	(total. claims - 20) x 18.00	\$.00
Multiple dependent claims	1.16(d)	(0 mult. dep. claims) x 270.00	\$	0.00
Filing Fee Calculation:			\$	710.00

3. Method of Payment of Fees

Charge Account No. 03-2357 in the amount of \$ 710.00. A duplicate of this transmittal is attached.

4. Authorization to Charge Additional Fees

The Commissioner is hereby authorized to charge any fees under 37 CFR 1.16 and 1.17 which may be required during the entire pendency of this application, to Deposit Account No. 03-2357.

5. Other papers enclosed

a) Return Receipt Postcard

Respectfully Submitted,

Dated: 10 30 00

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IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

PATENT APPLICATION

of

William Silver

for

METHOD AND APPARATUS FOR LOCATING OBJECTS USING UNIVERSAL ALIGNMENT TARGETS

Attorney Docket Number: C00-057

Express Mail Certificate Number: EM 067 610 794 US

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Method and Apparatus for Locating Objects Using Universal Alignment Targets

Related Application Data:

This application claims priority to Provisional Patent Application No. 60/162,521, filed in the U.S. Patent and Trademark Office on October 29, 1999, the content of which is hereby expressly incorporated by reference herein in its entirety.

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Field of the Invention:

This invention relates to automated visual alignment, and particularly to locating objects using automated visual alignment.

Background of the Invention:

The ability to determine the position and/or attitude of an object is of considerable practical importance in many applications, including industrial manufacturing, robot guidance, intelligent transportation systems, mail and parcel handling, and many others. Position might

include up to three degrees of freedom (e.g., up-down, in-out, and side-ways), and the three 1 degrees of freedom of attitude (e.g., pitch, yaw, and roll). Together, these six degrees of freedom 2 can be used to describe what can be referred to as the "location" or "pose" of an object. Note 3 4 that here, "location" or "pose" can mean more than just position in three spatial dimensions – it 5 can also include information as to the other non-translational degrees of freedom, such as skew, perspective, aspect-ratio, and many other more exotic non-translational degrees of freedom. In a 6 two-dimensional plane, position includes two translation degrees of freedom (e.g., up-down and 7 side-ways), and at least one non-translation degree of freedom, such as "orientation" (a rotation 8 9 degree of freedom), and possibly skew, aspect ratio, size, and others.

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It is well-known to use machine vision to locate objects at a distance. A digital image of a scene containing an object to be located is formed by any suitable apparatus, for example consisting of visible light illumination, a CCD camera, and a video digitizer. The digital image is then analyzed by a suitable image analysis device, for example consisting of a digital signal processor or personal computer running software that implements a suitable method for identifying and locating image patterns that correspond to the object of interest. The analysis results in certain parameters that describe the pattern in the image that corresponds to the object, or a suitable portion of the object, in the scene. These parameters might include position, attitude, and size of the pattern in the image. These parameters are then used to compute the location (pose) of the object using well-known mathematical formulas.

There are many methods known in the art for analyzing digital images to determine one or more of the pattern parameters, including blob analysis, normalized correlation, Hough transforms, and geometric pattern matching. Numerous other methods have been used or proposed in commercial practice or in academic literature.

The process of determining object location (pose) by machine vision can be referred to in various ways, including "alignment", "registration", "pattern recognition", and "pattern matching". For present purposes herein, those terms are equivalent, and so herein the term "alignment" shall be used to refer to any such process. Any object, or portion of an object, that gives rise to the pattern in the image to be analyzed shall be called an "alignment target", or simply a "target".

Most machine vision alignment applications require locating targets having a shape determined by engineering considerations that are largely independent of the needs of automated visual alignment. In these cases, the objects contain no special markings or components specially adapted to aid the alignment method. Consequently, the alignment method must work with whatever object shape is given. There are many applications, however, where the alignment target can be engineered specifically for that purpose. Examples include fiducial marks on printed circuit boards, registration marks etched on silicon wafers, and "bull's eye" targets used by the United Parcel Service on package labels. A target that has been engineered to aid machine vision alignment can be called a "cooperative target." In contexts where it is clear that a target has been engineered for alignment, the modifier "cooperative" is sometimes omitted, but "cooperative" is understood.

Although alignment methods have an extensive literature and commercial history, relatively little work has been done on understanding the effect of target shape on alignment performance. The work is almost entirely restricted to shapes composed of circles and polygons, to the effect of such shapes on binary image analysis methods, to translation-only (i.e., horizontal and vertical) alignment, and to accuracy criteria only.

Rotationally symmetric targets, primarily circles and "bull's-eye" patterns, have long been a favorite in the academic literature. In a 1974 paper, for example, W. Makous "Optimal Patterns for Alignment", in Applied Optics, Vol. 13, No. 3, states that "a bull's-eye pattern of regularly alternating black and white rings would be optimal for visual alignment in two dimensions." Twenty four years later, in a 1998 paper entitled "Design of Shapes for Precise Image Registration", in IEEE Trans. on Information Theory, Vol. 44, No. 7, Bruckstein, O'Gorman, and Orlitsky state that "Experimental tests and ... theoretical developments ... led to the conclusion that the 'bull's-eye' fiducial is indeed a very good, robust and practical location mark."

Rotationally symmetric targets suffer from a number of limitations, however, that have not been anticipated in the prior art. First, such targets contain no information for measuring orientation. This has been considered an advantage, based on the assumption that alignment methods would fail under orientation misalignment unless the target is rotationally symmetric,

but the recent advent of practical methods for orientation alignment have created a need for
 targets that convey substantial orientation information.

A second limitation of rotationally symmetric targets, such as the "bull's eye" pattern, is that circles and arcs of circles are extremely common in manufactured items, and one cannot guarantee that such shapes will not appear in the field of view containing the target. The appearance of such a shape in the same field of view as a target composed of circles or arcs of circles results in potential confusion for the alignment method, and this confusion usually leads to higher recognition error rates under variations in image quality typically encountered in an industrial environment.

A third limitation of rotationally symmetric targets is that they are often not good choices for measuring size, what might be called "size alignment". While such a target does contain plenty of information for conveying size, the concentric circular boundaries match each other perfectly at many different sizes. At the correct size the overall target match will be higher than at any of the wrong sizes, but the matches at the wrong sizes are sometimes good enough to create confusion under realistic conditions of image degradation. This "self-confusion" can lead to higher recognition error rates. Furthermore, this self-confusion generally requires that any practical alignment method must examine the "size" degree of freedom more carefully to avoid error, which increases recognition time.

The academic literature has also considered using as alignment targets simple polygons such as squares and diamonds, as well as complex sequences of stripes that are optimal for 1D or 2D alignment in some theoretical sense, but are almost impossible to manufacture.

Known targets in commercial use include simple geometric shapes such as circles, bull'seyes, squares, crosses, two squares touching at a corner, and patterns consisting of a cross embedded in a circle.

In the semiconductor industry, significant attention has been given to the engineering of targets used to achieve the extreme accuracy needed to register the many layers created during wafer processing. Early targets consisted of interleaved comb structures, which were used by human operators in manual alignment systems prior to the advent of machine vision alignment.

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- 1 More recently, manufacturers have used squares, concentric "box-in-box" shapes, crosses,
- 2 circles, rings, bull's-eyes, and various other shapes comprised of rectilinear or circular features.
- 3 Much of the prior art in semiconductors is concerned with process issues such as 3D structure,
- 4 edge profiles, circuit design rules, and resist flow.
- 5 Prior art cooperative targets suffer from one or more of the following limitations:
 - Target features are sometimes inadequate for providing sufficient information regarding non-translation degrees of freedom (e.g., orientation and size).
 - Reduced information is available when straight-line features are aligned (accidentally or otherwise) with the pixel grid.
 - Confusion and consequent reduced reliability result from use of circles, circular arcs,
 line segments, or right angles, which are common in manufactured objects, and
 therefore may be confused by the alignment method with other patterns in the scene.
 - Reduced reliability results from use of fine target features that do not survive a manufacturing process.
 - Confusion and consequent reduced reliability result from target shapes that are "self-confusing", i.e., that match themselves too well when translated, rotated, or changed in size.
 - Reduced alignment speed results from target shapes that cannot be identified unambiguously by their coarsest features.

For a number of reasons these limitations generally have not been serious for past use of machine vision. The alignment methods that have been available in the past, such as blob analysis and normalized correlation, had not been accurate enough (i.e., could extract only limited information from an image) to expose subtle limitations of the targets. Few practical methods existed for determining non-translation degrees of freedom, and those that were known were not widely used due to cost, reliability, or performance problems. Machine vision was often a new and challenging manufacturing technology, and so emphasis was placed on basic

- functionality and not on squeezing high performance from the equipment. In electronics and
- 2 semiconductor applications, among the largest users of machine vision, the coarser device
- 3 geometries of the past placed limited demands on machine vision alignment.

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PERSONAL PROPERTY

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- 4 Recent developments have created a need for a new breed of cooperative targets:
- The commercial availability of practical, highly accurate alignment methods capable of aligning non-translation degrees of freedom, including orientation and size, has created a
- 7 need for targets engineered to provide sufficient information in all such degrees of freedom.
 - Expanding experience with machine vision alignment has shown that increased error rates often result from targets that can be confused with similar shapes in the field of view, or are self-confusing in one or more degrees of freedom. Thus, there is a need for targets not based on common features such as lines, right-angles, and circles, and for targets specifically engineered to minimize or eliminate self-confusion in all degrees of freedom.
 - Shrinking sizes and tighter tolerances in manufactured goods, particularly in semiconductors and electronics, are placing increasing demands on accuracy, speed, and robustness of machine vision alignment. Consequently, there is a need to reconsider the often-neglected role of target shape, and produce targets that cooperate with practical alignment methods to achieve best performance.

The need for new cooperative targets not subject to the limitations of the prior art leads to a need for new methods for engineering such targets. Prior art methods for engineering targets suffer from one or more of the following limitations:

- The known target engineering methods address only translation alignment, not other degrees of freedom such as orientation and size.
- The known target engineering methods are based on a theoretical analysis of absolute accuracy, which to avoid intractable complexity, requires unrealistic simplifying assumptions about image quality, requires that target shape be restricted to simple shapes composed of circles and rectilinear edges, and requires the use of simple binary alignment methods, such as blob centroid.

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- 2 The known target engineering methods do not consider alignment reliability under
- 3 practical conditions of image variation and process degradation.

The known target engineering methods do not consider alignment speed.

- The known target engineering methods do not consider confusion with other patterns and self-confusion.
- 6 Consequently there is a need for a new method for engineering alignment targets.

Another factor contributing to reduced performance of known cooperative alignment targets is insufficient precision in known methods for rendering such targets. Without the ability to render a cooperative alignment target at very high precision, an alignment target engineered to address the problems of the prior art would not perform optimally. Consequently, it is necessary to be able to render such targets in various forms, including bitmap images, at very high precision. In the prior art, methods for rendering shapes accurately on a discrete grid have been studied extensively for graphics applications, where they are generally referred to as anti-aliasing methods. These methods produce pleasing graphics for human observation, but achieving the extreme accuracy and flexibility needed for machine vision alignment applications is difficult.

In the machine vision prior art, several methods have been used to render binary shapes on discrete grids. In one method, pixels along the shape boundary are given a gray value corresponding to the fraction of the pixel's area that falls on either side of the boundary. This method suffers from several limitations:

- The computations are complex, resulting in very slow rendering that makes automated testing using thousands of synthetically generated images impractical.
- The method assumes an unrealistically ideal sensor model, resulting in loss of accuracy. Attempts to improve the sensor model by post-processing the rendered image are also limited in accuracy due to grid quantization.
- The method is impractical for complex shapes that are not composed of straight-line segments.

In another known rendering method, a binary image is rendered at much higher resolution than that needed for the target rendering. This high-resolution image is then filtered and subsampled to produce the final rendering. While such a method can be quite accurate in principal, computer time and memory limitations make truly high accuracy impractical.

Summary of the Invention

It is well-known in the prior art to cause a cooperative target to appear on an object to be located, place the object within the field of view of a camera or other suitable image formation device, capture an image of the object bearing the target, and analyze the image using an alignment method to determine the x-y position of the target in the image.

The invention includes a method and apparatus for locating objects by means of machine vision alignment using cooperative targets. The method and apparatus provides significant improvements over the prior art. In one general aspect, the invention uses novel cooperative targets that have substantial performance advantages over those used in the prior art. In another general aspect, the invention uses alignment methods having non-translation alignment capabilities, such as geometric pattern recognition, cooperating with suitable targets to perform alignment in non-translation degrees of freedom, such as orientation and size.

The invention includes a novel set of criteria for evaluating alignment targets for accuracy, speed, yield (robustness), and ease of use. The accuracy criteria of the invention are based on a quantitative analysis of target boundary shape that has several advantages over prior art methods:

- The accuracy criteria of the invention can be used for essentially arbitrary shapes;
- The accuracy criteria of the invention provide estimates of the information content of a cooperative target, independent of any specific alignment method; and
- The accuracy criteria of the invention can evaluate targets for their capacity to accurately align non-translation degrees of freedom, such as orientation and size.

The accuracy criteria of the invention also include a quantitative measure of the tendency of a target to contribute to loss of accuracy due to accidental alignment with the pixel grid of the machine vision system, a phenomenon referred to herein as "grid degeneracy". This phenomenon has been recognized in academic research, although useful remedies appear not to have been investigated, and many cooperative targets in current use suffer from this problem.

Although speed criteria are apparently unknown in the prior art, an aspect of the invention includes qualitative criteria based on certain common characteristics of most practical alignment methods in use, which are in turn loosely based on principals of information content.

Yield criteria are also apparently unknown in the prior art, with the exception of targets used for wafer fabrication in the semiconductor industry, where the criteria are specific to wafer processing. For high yield (low error rates), an aspect of the invention considers the ability to survive manufacturing processes and other environmental conditions. Another aspect of the invention includes criteria relating to potential errors caused by self-confusion and background confusion.

The ease-of-use criteria of the invention require that targets be easy to render on the objects to be located, easy to teach to the machine vision alignment method, and easy to analyze using the criteria of the invention. To satisfy these ease-of-use criteria, the invention uses targets that are defined by a set of algebraic formulas.

The invention includes a novel method of accurately rendering algebraically defined shapes that can be used to render alignment targets, or for other purposes. The method can render shapes as a bitmap image for machine vision alignment training, for computer display for human observation, and for computer printout for documentation. The method can aid in rendering targets on the objects to be located by providing input to a computer-aided design (CAD) system, or by directly controlling devices such as laser engravers. The rendering method of the invention is fast, extremely accurate, and can handle substantially arbitrary shapes.

The rendering method according to the invention includes two key steps: first, targets are defined by a real-valued function of position in the real plane that gives the distance from that position to the nearest point on a target boundary. The function gives distance as a positive value

1 for points inside the figure, and as a negative value for points outside the figure; and second, an edge model is used to map distance to real-valued image intensity. By choosing appropriate edge 2 3 model parameters, edge sharpness, focus, video gain, and noise can be modeled. Other steps are 4 used with these two key steps to provide a complete rendering method. In a preferred 5 embodiment, the rendering method of the invention uses high-precision floating point arithmetic 6 to estimate real-valued functions on the real plane, and only converts to a discrete grid as the 7 final step. The result is the ability to control the position, orientation, and size of the final 8 rendering to extremely high precision.

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The invention includes a novel method for engineering alignment targets that satisfy the above set of criteria of the invention. By contrast, known methods generally try to analyze a set of specific shapes, such as a circle, square, and diamond, and then simply choose the best one. Alternatively, in some known methods, a single parameter such as aspect ratio might be optimized according to some criteria. The method of the invention for engineering alignment targets, by contrast, starts with a simple shape and then refines the initial shape in a series of steps, where each such step produces a different shape, derived from the previous step, that resolves some deficiency of that shape.

In one embodiment of the method for engineering alignment targets, the initial shape contains radial features, which carry orientation information but not size, and circular features, which carry size information but not orientation. As recognized by the invention, this independence of radial and circular features allows orientation and size performance to be adjusted independently.

In another embodiment of the method, the starting shape is defined algebraically using polar coordinates. In a preferred embodiment, the starting shape is a "fan".

In a preferred embodiment, the series of steps includes at least one step whose purpose is to achieve at least one of the following goals:

Increase boundary perimeter to improve accuracy. In a preferred embodiment,
 perimeter is increased by adding holes.

1 They satisfy the invention's evaluation criteria. 2 They result from the use of the invention's engineering method. 3 They have no significant rotational symmetry. They have no significant orientation or size self-similarity. 4 5 They are not primarily composed of circles, circular arcs, straight lines, or right 6 angles. 7 In one embodiment, the specific alignment targets are shapes consisting of at least one "generalized polar polygon." A generalized polar polygon is a plane figure that is a polygon with 8 9 optionally rounded vertices when drawn in polar coordinates, keeping in mind that all 面面也沒多 coordinates (r, θ + 360°n), for integer n, are the same point. Such a figure will include radial lines, circular arcs, and spiral segments when drawn in the Cartesian plane. In another embodiment, the specific alignment targets are members of a family of "fan" shapes. 14 In a preferred embodiment, the targets are fan shapes that satisfy all, or almost all, of the 15 16 evaluation criteria established by the invention. These are novel shapes that have no prior history in mathematics or practical arts. Any target that substantially satisfies all of the evaluation ij criteria is called a "Universal Alignment Target" (UAT). 18 19

Brief Description of the Drawings

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The invention will be more fully understood from the following detailed description, in conjunction with the following figures, wherein:

- Figure 1 shows a typical cooperative target in common use, and illustrates some of the basic 22
- 23 properties of targets considered by the invention.
- 24 Figure 2 illustrates how the figures of merit used for the accuracy criteria are computed.

- Figure 3 illustrates an accidental alignment of a target to the machine vision system's pixel grid,
- which results in loss of information called a "grid degeneracy".
- 3 Figure 4 illustrates the alignment speed criteria.
- 4 Figure 5 illustrates the alignment yield criteria.
- 5 Figure 6 illustrates a target defined by a set of algebraic formulas to satisfy the ease of use
- 6 criteria.
- 7 Figure 7 illustrates a preferred rendering method according to the invention.
- 8 Figure 8 shows an edge model used in a preferred embodiment of the rendering method.
- Figure 9 illustrates some common alignment targets that are used as a reference point in the engineering of novel, high performance targets according to the invention.
 - Figure 10 illustrates a starting shape, the "primitive fan", according to a preferred embodiment of the target engineering method of the invention.
 - Figure 11 shows the first refinement in the fan series, the "simple fan".
 - Figure 12 illustrates the next refinement step, the "balanced fan."
 - Figure 13 illustrates the next refinement, the "balanced asymmetric fan."
- 16 Figure 14 illustrates the next refinement, the first version of the "balanced radically asymmetric
- 17 fan."

- 18 Figure 15 illustrates the final alignment target shape, the "balanced radically asymmetric fan",
- which is considered a superb universal alignment target.
- 20 Figure 16 illustrates an apparatus for locating objects using cooperative targets.

Detailed Description of the Drawings

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- 2 Figure 1 shows a typical cooperative target in common use, and illustrates some of the basic
- 3 properties of targets considered by the invention.
- 4 Practical targets are characterized by discontinuities of some quantity (i.e. brightness, texture) at
- 5 some appropriate granularity (spatial resolution). These discontinuities are boundary contours 100
- 6 (sometimes called edges), physical or subjective, that separate roughly uniform regions 110 and
- 7 120. Although it is possible to imagine targets with no uniform regions and no discontinuities,
- 8 they are hard to fabricate and generally unreliable due to the well-known observation that image
- 9 shading is much less consistent under real-world variations than the shape and position of the
- 10 boundaries. Thus from this point forward we consider only targets characterized by boundaries
- separating roughly uniform regions.

We avoid all consideration of shading in the engineering of a target and consider only the shape of the boundaries. All shadings that can produce the boundaries are considered equivalent, and for simplicity we assume binary shading on the real plane. When targets are rendered on a discrete grid, however, the boundaries must be carefully shaded in gray-scale to convey accurate boundary position and orientation information.

Information about a target's position is to be found exclusively along the boundary contours, for example 100. In uniform or uniformly-varying regions, for example 110 and 120, no position information is available for the simple reason that all points is such regions look the same. This is a fact of geometry that is independent of the alignment method—even area-based methods such as normalized correlation ultimately get their position information from these boundaries.

22 It is well-known that the shape of the boundary contours has some bearing on the ability of a

target to provide information for specific degrees of freedom. For example it has long been

observed that a circle cannot be used to measure rotation, a corner cannot be used to measure

size, and a rectangle provides more translation information normal to its long axis than its short

26 axis. These bits of intuition can be formalized, resulting in formulas for computing figures of

merit that allow one to assess quantitatively the ability of a given shape to measure a given

degree of freedom. The figures of merit are non-negative unbounded real numbers. For rotation

- 1 and size, a single number each is defined. For translation, the figure of merit is a function of
- 2 direction.

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- 3 Alignment accuracy is determined by a combination of factors, the most important being the
- 4 intrinsic capabilities of the alignment method, the information content of the target, and the
- 5 magnitude of image degradation. The figures of merit measure the information content of the
- 6 target only, and thus do not directly determine accuracy. Their value is that they allow targets to
- 7 be compared quantitatively and independent of the alignment method in use.
- 8 Figure 2 illustrates how the figures of merit are computed. Let the parameter s be arc length
- 9 along a contour. Consider a small segment 200 of contour of length ds, at position defined by the
- 10 vector $\mathbf{p}(s)$ 210 relative to some point \mathbf{cp} 220. Define the unit vector $\mathbf{u}(s)$ 240 normal to the
- 11 contour at **p**, and the unit vector $\mathbf{u}(\theta)$ 230 in direction θ , all as shown in figure 2.

The contribution to the figure of merit of a given degree of freedom by the segment is the area swept out by the segment per unit change in the degree of freedom. For rotation and size the change is about the point cp, further defined below. Thus segments oriented parallel to the direction of motion induced by a change in the degree of freedom sweep no area and contribute nothing to the figure of merit, and segments oriented normal to the direction of motion contribute the most. For rotation and size, the contribution is proportional to distance from **cp**, which is consistent with one's intuition.

From this discussion, the rotation, size, and translation figures of merit for any contour can be written as follows (note that the vector cross product in 2 dimensions produces a scalar):

$$R = \oint |\mathbf{u}(s) \times \mathbf{p}(s)| ds \tag{1}$$

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$$R = \oint |\mathbf{u}(s) \times \mathbf{p}(s)| ds$$
 (1)
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$$S = \oint |\mathbf{u}(s) \cdot \mathbf{p}(s)| ds$$
 (2)
23
$$T(\theta) = \oint |\mathbf{u}(s) \cdot \mathbf{u}(\theta)| ds$$
 (3)

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$$T(\theta) = \oint |\mathbf{u}(s) \cdot \mathbf{u}(\theta)| ds \tag{3}$$

- 24 R and S are meaningless without a suitable choice for cp. Indeed one could make R and S
- 25 arbitrarily large for any contour simply by choosing cp to be far away. One useful choice is the

- 1 geometric point that minimizes the integral of squared distance between it and lines passing
- 2 through and normal to the contour, which we call the center of projection. The center of
- 3 projection can be computed as follows, where the x and y subscripts denote components of a
- 4 vector:

$$q(s) = \mathbf{p}(s) \bullet \mathbf{u}(s) \tag{4}$$

$$g = \oint u_x^2(s) ds \oint u_y^2(s) ds - \left[\oint u_x(s) u_y(s) ds \right]$$
 (5)

$$cp_{x} = \left[\oint q(s)u_{x}(s)ds \oint u_{y}^{2}(s)ds - \oint q(s)u_{y}(s)ds \oint u_{x}(s)u_{y}(s)ds \right]/g$$
 (6a)

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$$cp_{y} = \left[\oint q(s)u_{y}(s)ds \oint u_{x}^{2}(s)ds - \oint q(s)u_{x}(s)ds \oint u_{x}(s)u_{y}(s)ds \right]/g$$
 (6b)

Figure 3 illustrates an accidental alignment of a target to the machine vision system's pixel grid, which results in loss of information as discussed in the following paragraphs.

The figures of merit consider targets to be continuous boundary contours in the real plane. This is fine for analysis, but in practice images are represented as values on a discrete grid, for example 300. Unlike the real plane a grid is distinctly anisotropic—it has special directions, parallel to the grid axes and, to a lesser extent, parallel to the diagonals, which affect the information-bearing capacity of target boundaries that line up along those directions. The effect is subtle but significant, particularly for alignment methods with high intrinsic accuracy.

Consider the one-dimensional image intensity profile normal to a boundary contour, for example 310, 320, or 340, at some point. If the boundary moves by a whole pixel amount, the profile shifts correspondingly but its shape is unchanged. For fractional pixel shifts the profile shape changes, so that the shape of the profile encodes information about sub-pixel position, although there are practical limits on how much information can be extracted at any given point. If we consider the information provided by many such profiles at many points along the boundary, however, a significant improvement in position information content can be obtained, but *only if the various boundary points represent statistically independent measurements*.

- 1 If a target boundary cuts the pixel grid 300 in a random or pseudo-random manner, for example 2 320 and 340, statistical independence is high and maximum information is conveyed. On the other 3 hand, if a portion of a boundary contour happens to line up parallel to a grid axis, for example 4 310, the intensity profile shapes at points along that portion are necessarily identical (except for 5 measurement noise), and therefore provide no mutually independent information. It is as if only 6 one point along the boundary portion is considered instead of many. Such an accidental 7 alignment of target 310 to grid 300, and the resulting loss of information, is called a grid 8 degeneracy. Grid degeneracy in principle affects any alignment method, whether intensity 9 profiles are examined directly or only indirectly, but is most noticeable when the alignment 10 method's intrinsic accuracy is very high. 11 The loss of accuracy associated with grid degeneracy is not always apparent. Some alignment 12 methods do not have sufficient intrinsic accuracy for the effect to be measurable. In other cases, a method may use a model of intensity profile shape that happens to match well the behavior of specific images being tested. This may mask the grid degeneracy for those images, but since profile behavior is not reliable to high precision such a result is unreliable in practice. Targets such as crosses, for example 310 and 320, and rectangles suffer most seriously from grid degeneracies because the entire boundary can be aligned simultaneously with the grid axes, as in 310. The worst case for such figures occurs when the target dimensions are close to a whole number of pixels, because no independent measurements are made anywhere along the entire boundary. If the dimensions are not close to a whole number of pixels, then at least some 21 independent information can be obtained from different edges of the target (e.g. the left and right 22 side of a rectangle). 23 Susceptibility to grid degeneracy is an important accuracy criterion in the engineering of an 24 alignment target. A figure of merit GD one can use is the fraction of the target's boundary
- contours that can align with the pixel grid simultaneously. For rectangles and crosses GD is 1.0, the worst case. For circles 340 it is 0, the best case. Note that this figure of merit doesn't consider the effect of whole pixel dimensions.
- Figure 4 illustrates the alignment speed criteria used, as further discussed in the following paragraphs.

- 1 For most practical alignment methods, the most important effect on speed of the engineering of a
- 2 target is the extent to which the target can be identified unambiguously by its coarse features.
- 3 This criterion is hard to quantify meaningfully, and so is more a matter of judgement. Fine detail
- 4 itself is not a problem, but for best alignment speed it should be used to enhance accuracy and
- 5 not to identify the target.
- 6 For example the thin cross 400 fails to satisfy this criterion, and is a poor choice for an alignment
- 7 target. The cross 400 has only fine detail, no coarse features that can be used to estimate its
- 8 location in a coarse resolution examination of the image.
- 9 Unambiguous identity based on coarse features applies to each of the degrees of freedom.
- 10 Consider for example the target 420. The x-y position of this target is unambiguous when looking
- at its coarsest feature, the overall square shape. Its orientation, on the other hand, has 90°
 - ambiguities until one looks at its finest feature 430. Although one should expect an alignment
 - method to be able to determine the rotation of this target over a 0 360° range, the alignment
 - time will be longer because fine detail must be examined in order to do so. Note that target 400
 - fails the speed criterion in all degrees of freedom.
 - Figure 5 illustrates the alignment yield criteria used, as further discussed in the following
 - paragraphs.

- In general the most significant factor affecting alignment yield is image degradation—if images
- were always perfect copies of the trained pattern, just about any alignment method would give
- 20 100% yield. Although image degradation may be intrinsic to the manufacturing process and
- 21 difficult to control, there are some target engineering criteria that can help.
- 22 One form of degradation is where the target fails to survive the manufacturing process
- reasonably intact. For the most part survivability is an application-specific issue, but we can
- reasonably assume in general that coarse features will survive better than fine features. This is
- 25 consistent with and perhaps more restrictive than the speed criterion, suggesting that at least for a
- 26 UAT very fine features should be avoided.
- 27 The effects of degradation are mitigated when the target's shape is as dissimilar as possible both
- from other patterns in the field of view and from translated, rotated, or sized versions of the

- 1 target itself (i.e., low auto-correlation secondary peak in all degrees of freedom). If the target is
- 2 too similar in appearance to other patterns or itself, image degradation can wipe out differences
- 3 and cause failures to find or misalignments. For example the target 420 is very similar to itself in
- 4 90° rotations. If image quality degrades significantly as in 500, the small difference 510 between
- 5 the correct and false orientations can be hard to detect reliably.
- 6 Another example of self-similarity is a triangle in the size degree of freedom. Fully two-thirds of
- 7 the boundary of a triangle will match a larger version of the same shape.
- 8 Similarity to other patterns in the field of view is of course application-specific, but again general
- 9 guidelines are possible. Parallel and orthogonal features, and simple geometric shapes, are
- 10 common in manufactured goods and are therefore best avoided in an alignment target intended to
- 11 be universal.
 - Consider for example a portion of a printed circuit board 530 containing circuit traces 550 and an
 - alignment target 540. Note that the traces in area 560 match 75% of the target 540. As long as
 - image quality is near perfect the false target 560 can be distinguished from the real target 540.
 - Under realistic conditions of image degradation, however, the similarity of area 560 to target 540
 - will result in a non-zero error rate.
 - Figure 6 illustrates a target defined by a set of algebraic formulas to satisfy the ease of use
 - criteria, as further discussed in the following paragraphs.
- An alignment target should be easy to render, train, and analyze. Training includes both
- 20 producing suitable shape information for an alignment method and selecting a known reference
- 21 point on the target for reporting alignment position. Analysis includes computing the figures of
- 22 merit.

- 23 Since all alignment methods in common use can be trained from images, and since there is no
- 24 other generally accepted format for providing shape information, a high quality pixel-grid
- 25 rendering of a target is considered necessary and sufficient for training a target. Realistically
- shaded edges are considered essential for providing accurate shape information, so for example
- targets generated by the typical "paint" programs are unacceptable.

- 1 Targets drawn by hand using painting or drawing programs, or acquired from a physical device
- 2 such as a video camera, are difficult to analyze, usually do not allow precise selection of a
- 3 reference point, and may be difficult to render in whatever substrate will contain the target in the
- 4 alignment application. Such targets are not suitable for use as a UAT.
- 5 The objectives are met by targets that are defined algebraically in the real plane. In a preferred
- 6 embodiment, a target is defined by a real-valued function of real-valued coordinates f(x, y) such
- 7 that f gives at each point (x, y) the distance and direction (+ or -) to the nearest boundary
- 8 contour. The contours are defined by f(x, y) = 0, the points inside the contours as f(x, y) > 0, and
- 9 outside as f(x, y) < 0.

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- For computational simplicity the method does not require that f(x, y) give precise distance, only
- that the value is reasonably close. This simplification has been found useful for targets best
 - defined in polar coordinates, such as the fan configurations, which are derived from the
 - function's Cartesian arguments.

For example target 600 is a square of radius 610 r, and with corners rounded to radius 620 c. The target is defined according to a preferred embodiment by defining the function f using the set of algebraic formulas 630.

A set of algebraic formulas defining a target provides a universal and unambiguous definition, which can serve as the basis for a computer program that can render the target for various purposes:

Training

The rendering program can produce a bitmap image that can be fed directly to an alignment method for training. The target reference point is also defined algebraically. As a result, training is fully automatic, with no human involvement and no need to even acquire a training image from a camera.

Reproduction

The rendering program can be used to reproduce the target on the substrate used in the alignment application. Source code for the program can be delivered to manufacturers of CAD systems, laser engravers, and the like for use in their products. Source code is absolutely precise and

1		unambiguous, can be independently tested and certified, can be distributed			
2		by email or published on Web sites, and is ultimately what just about any			
3		mechanical rendering device will need. Of course what makes a target			
4		easy to render is somewhat application-specific. For example, some			
5		processes may be able to render only horizontal and vertical features.			
6		Nevertheless algebraically-defined targets with appropriate software are			
7		flexible enough to handle most application-specific requirements.			
8	Documentation	The rendering program can produce pictures of the target for written			
9		documentation, as was done in the production of this patent specification.			
10	Analysis	The rendering program is used to drive analysis software that computes			
11		figures of merit by numerical integration. Since the rendering program			
12		itself drives the numerical integration, the results are guaranteed to			
		correspond to the target as rendered.			
14	Testing	The target is defined on the real plane and the rendering program			
15		approximates this using high-precision floating point calculations. As a			
16		result the target can be translated, rotated, and sized to effectively arbitrary			
17		precision prior to rendering as a discrete image. Various edge, lens, and			
18		noise models can be applied in the floating point domain. The resulting			
		images can be used for fully automated accuracy, speed, and yield testing.			
20	Figure 7 illustrates a	preferred rendering method according to the invention. This method for			
21	algebraic rendering	and analysis of targets has been found by experience to be remarkably			
22	simple, as measured	in number of lines of code needed, and in general, as measured by the			
23	variety of targets tha	t can be generated. Following the preferred method, a target is defined by a			
24	real-valued function	of real-valued coordinates f(x, y) as described above and illustrated by			
25	example in figure 6.				
26	A scan pattern gener	ration step 700 is used to generate a sequence of real-valued coordinates (x, y)			
27	as appropriate for the rendering to be made. For example, to render a bitmap image the				

- 2 the coordinates would correspond to beam position.
- 3 An optional lens model step 710 is used to apply a coordinate transform to model the imaging
- 4 geometry, which maps the scan pattern coordinates (x, y) to new coordinates (x', y'). Typically
- 5 an identity transform is used, but translation, rotation, size, aspect ratio, skew, perspective, and
- 6 lens distortion transforms can be applied. These transforms are of particular value for alignment
- 7 method accuracy testing, because the amount of transformation is precisely known.
- 8 A computational step 720 is used to compute the shape-defining function f(x', y'), which results
- 9 in a real-values estimate of distance to the nearest boundary contour.
- 10 An edge model step 730 is used to apply a real-valued brightness transform that models edge sharpness, focus, video gain, noise, and other physical processes.
 - A digitizer model step 740 is used to convert the brightness values I as appropriate for the final rendering, for example 8-bit integers for monochrome bitmap images 750.
 - The only target-specific software needed is the code to implement the function f(x, y) in step 720.
 - The above example target of figure 6 requires around 20 lines of code in the Visual Basic
 - programming language; the complex UAT shown in figure 15 requires around 200.
 - Target-independent software follows the target contours defined by f(x, y) = 0 and performs the
 - numerical integration needed to compute the figures of merit. A small amount of target-specific
- 19 software to provide a list of contour starting points is used. The contour following software can
- 20 also generate a line-drawing of the target if such is needed.
- 21 A system for target generation follows an object-oriented approach with targets implemented by
- 22 polymorphic objects and used by target-independent rendering and analysis software. Such a
- system would include a GUI for parameter selection and display of images and other results. 23
- 24 The above description relies on hard-coded implementations of f(x, y), which results in high
- 25 rendering speed and simple software design. It is also possible to implement a "universal"
- 26 function f_u that uses a general-purpose shape description in the form of lines and arcs, such as a

- 1 CAD description. With such a method creating a new target shape would be simpler and require
- 2 no programming, but a larger one-time software effort would be needed to implement f_u and
- 3 rendering and analysis would be slower. A complete system for target generation would include
- 4 both universal and specialized functions.
- 5 Figure 8 shows an edge model used in a preferred embodiment of rendering step 730. The figure
- 6 shows the f coordinate axis 800, which represents distance (+ or –) to the nearest boundary
- 7 contour, and the brightness coordinate axis 820. In a preferred embodiment, a sigmoid function
- 8 **840** is used:

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$$I = background + \frac{contrast}{1 + e^{-t/\sigma}}$$
 (7)

This edge model is easy and fast to compute, produces excellent anti-aliased edges, and allows precise control of edge sharpness using the parameter σ .

Figure 9 illustrates some common alignment targets that are used as a reference point in the engineering of novel, high performance targets according to the invention. For clarity we start with simple geometric shapes and build in small steps towards the goal. It should be clear that the resulting UAT is not unique, and that many variations, both minor and substantial, would be consistent with the spirit of the procedure and may be more suitable for specific applications.

Speed and yield criteria are based on an analysis of the degree of similarity between the target and other patterns. Similarity is somewhat dependent on the alignment method in use, particularly on whether the method is primarily based on areas, or on boundaries. While different methods may disagree on the degree of similarity between two patterns, in general there is necessarily much more agreement than disagreement.

- 22 In the following development, similarity is considered based on boundary matching, not area
- 23 matching. While the analysis is therefore more directly applicable to boundary-based methods, it
- 24 is still largely method independent since boundary shape determines area shape. The UAT that
- results is a superb target for use with just about any general-purpose method.
- Consider first a circle 900 of radius r. The figures of merit are given in table 1.

Table 1. Circle					
R	S	worst $T(\theta)$	best $T(\theta)$	GD	
0	$6.28 r^2$	4.0 r	4.0 r	0	

- 2 As can be seen there is no information for measuring rotation and no grid degeneracy. The scale
- 3 figure of merit is pretty good but the translation figure could be better. If we ignore the rotation
- 4 degree of freedom, speed and yield criteria are satisfied as long as no similar shapes appear in the
- 5 field of view. Circles are common shapes, however. Of course we don't need all of this analysis
- 6 to know that a circle is a poor choices for a UAT, but the numbers give a point of comparison
- 7 when considering other shapes.

Now consider a square 920 of radius r, whose figures of merit are given in table 2.

Table 2. Square					
R	S	worst $T(\theta)$	best $T(\theta)$	GD	
$4.0 r^2$	$8.0 r^2$	4.0 r @ 0°	5.66 r @ 45°	1.0	

All degrees of freedom can be measured, although twice as much information is available to measure size as rotation (these figures can be compared directly, but cannot meaningfully be compared with the translation figures). A factor of $\sqrt{2}$ imbalance also exists between the best and worst translation directions. These imbalances are not serious, but neither are they ideal. Grid degeneracy is worst case. Speed is good, but the square will match itself perfectly at 90° rotation increments, and 50% of its boundary will match a corner or a much larger square. These self-similarities, combined with the fact that it is a common shape, fail to satisfy our yield criteria.

Next consider a cross 940 of radius (half-width) r and arm radius (half-thickness) a, whose figures are given in table 3.

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Table 3. Cross					
R	S	worst $T(\theta)$	best $T(\theta)$	GD	
$4.0 r^2$	$8.0 \ a \ (2r-a)$	4.0 r @ 0°	5.66 r @ 45°	1.0	

- 1 Interestingly, except for the size degree of freedom the figures are identical to those of a square.
- 2 This makes sense since the boundaries of a cross are identical to those of a square in perimeter
- 3 length and orientation; a cross is just a square with its corners folded in. Considering just these
- 4 figures of merit, then, a cross is never better than a square, and always worse in size
- 5 measurement capability.

6 Other factors may come into play, however. Recall that GD does not capture the ability to 7 mitigate the effects of grid degeneracy by choosing the dimensions of the target to be non-whole-8 9 10 11 12 pixel amounts. With a square there are only two independent edges potentially providing translation information (it's not 4 because there are 2 translation degrees of freedom). With a cross with sufficiently thick arms, we get 4 edges for each translation degree of freedom, assuming that none of the 6 possible pairs of the 4 edges are separated by a whole number of pixels. Thus a cross can be made less susceptible to grid degeneracy than a square, but only by 13 14 15 careful engineering.

Another factor that might favor a cross is that in some applications scene real estate may be too limited to allow using a square, but a cross can be squeezed in between other portions of the scene.

- 17 Thin crosses fail to meet the speed criteria due to lack of coarse features, and all crosses suffer
- 18 from the same yield concerns as squares.
- 19 Since crosses are commonly used as alignment targets in spite of these problems, the above
- 20 analysis is summarized in the following guidelines for their use:
- 21 1. Make the arms as thick as possible
- 22 2. Make the edge-to-edge dimensions not be whole numbers of pixels.

- 3. Round the corners if possible to further reduce grid degeneracy.
- 2 Figure 10 illustrates a starting shape according to a preferred embodiment of the target
- 3 engineering method of the invention. This starting point and the shapes derived from it have
- 4 proven to be productive in engineering superb alignment targets. The shapes are based on a basic
- 5 shape-type that we call a fan. Other starting points and refinement decisions are possible, and no
- 6 implication is made that the fan shapes are best. They are the best we've developed to date,
- 7 however, and the principles used to engineer them can be applied in exploring other
- 8 configurations.

- 9 The primitive fan shape (primfan) is shown in figure 10. It consists of 4 blades 1000 connected to
- a central circular hub 1010. All inner and outer corners, for example 1020, are rounded to avoid
 - sharp corners that are hard to fabricate in many substrates, and often fail to survive harsh
- t2 environments

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- All of the fan shapes that are considered herein are defined by straight-line segments in polar coordinates. The vertices where these segments intersect are rounded by segments of circles, also in polar coordinates for simplicity. Thus the actual shape of the rounded corners in the final Cartesian rendering is complex, but for the small radii used they look just fine. A plane figure constructed from line segments in polar coordinates, with optionally rounded vertices, is called a generalized polar polygon.
- In figure 10 the primfan is also drawn in a polar coordinate system 1050. The blades 1060 and hub 1070 can be seen.
- Here and below the radius of the fan is r. The parameters defining this particular primfan are
- 22 given in table 4, and the figures of merit in table 5.

Table 4. Primfan parameters				
Fan radius	r			
hub radius	0.2 r			
blade width 1035	45°			
blade gap width 1030	45°			
corner radius	0.047 r			

Table 5. Primfan				
R	S	worst $T(\theta)$	best $T(\theta)$	GD
$3.84 r^2$	$3.27 r^2$	6.11 r @ 22.5°	6.50 r @ 0°	0.31

The worst case translation figure for the fan is better than the best case for circles, squares, and crosses of equal radius, and 53% better than the worst case for those targets. This is because more perimeter is packed into the same area, and better balanced in orientation. *GD* is pretty good at 0.31, corresponding to 4 of the 8 blade edges simultaneously subjected to grid degeneracy. The figures for rotation and size are a little small and somewhat imbalanced, but not bad either.

Speed is excellent due to unambiguous coarse features. There is of course the 90° symmetry, and self-similarity in size is also too large due to the fact that the radial features, which comprise 63% of the total perimeter, match perfectly as size changes. The fan is not a common shape, however, and is not likely to be confused with other patterns in the field of view.

Figure 11 shows the first refinement in the fan series. Holes 1100 are added in the blades, resulting in the simple fan shape 1110 (simfan), with hole parameters given in table 6 and figures of merit in table 7. The simfan is also drawn in polar coordinates 1120.

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Table 6. Simfan hole parameters				
hole inner radius	0.5 r			
hole outer radius	0.8 r			
hole width	15°			

- 1 The additional perimeter improves all of the figures of merit. R and S are somewhat more
- 2 imbalanced, though, as the defined boundary squeezes more information out of the rotation
- 3 degree of freedom than size.

Table 7. Simfan					
R	S	worst $T(\theta)$	best $T(\theta)$	GD	
$5.40 r^2$	$4.19 r^2$	8.20 r @ 45°	8.83 r @ 0°	0.24	

Speed is still expected to be excellent. The rotation 90° ambiguity hasn't been addressed, but the size self-similarities are reduced because the holes won't match at the wrong size.

Figure 12 illustrates the next refinement step. One advantage of the fan configuration is that since it is composed of radial and circular features, rotation and size performance can be controlled independently. With a simple change we can bring up S without affecting R. The result 1200 is called a *balanced fan* (balfan), also shown in polar coordinates 1220. The defining parameters given in table 8, and the figures of merit in table 9.

Table 8. Balfan parameters			
Fan radius	r		
hub radius	0.2 r		
blade width 1235	56°		
blade gap width 1230	34°		
corner radius	0.047 r		

hole inner radius	0.5 r
hole outer radius	0.8 r
hole width	18.67°

- 1 Note that all we've done is widen the blades to 56°, and widen the holes proportionally (the
- 2 holes are $1/3^{rd}$ the blade width).

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Table 9. Balfan			,	
R S worst $T(\theta)$ best $T(\theta)$ GD				
$5.40 r^2$	$5.15 r^2$	8.92 r @ 45°	9.31 r @ 0°	0.22

Note that the figures of merit are fairly well balanced, hence the name of the fan, and numerically better than simfan and much better than any of the simple geometric shapes we considered above. Speed and yield are neither better nor worse than simfan.

Figure 13 illustrates the next refinement, which is to fix the 90° ambiguity. This is done by making each blade and gap a different size. The resulting shape 1300 is called a *balanced* asymmetric fan (basfan), also shown in polar coordinates 1350. This basfan has the same total blade and gap width as the balfan, so that the figures of merit that we worked to balance are not significantly changed. As before the holes are kept at $1/3^{rd}$ the blade width.

The parameters describing the blades are given in tables 10a and 10b, with figures of merit in table 11. All of the radial and rounding parameters are as for previous fans.

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Table 10a. Basfan parameters				
Blade	Blade Starting Azimuth			
1310, 1360	0°	38°		
1320, 1370	57°	50°		
1330, 1380	146°	74°		
1340, 1390	269°	62°		

Table 11. Basfan				
R	S worst $T(\theta)$ best $T(\theta)$ GD			
$5.42 r^2$	5.21 r ²	8.64 r @ 38°	9.47 r @ 134°	0.11

Note, as expected, that R and S are not significantly changed from balfan. The worst case $T(\theta)$ has dropped slightly, with the best case rising, which is not surprising. GD has gone down by half, since now no more than two blade edges can suffer simultaneously from grid degeneracy. Note that with 8 blade edges and 28 pairs it is essentially impossible to reduce this to just one edge, since the test for simultaneous grid alignment has to allow for approximate alignment.

Although we've eliminated the serious 90° ambiguity, there is still some rotation and size selfsimilarity in the basfan. Considering rotation, any blade edge will match any other at some angle, and any point on the circumference will match any other point on the circumference. The asymmetry of the basfan reduces but does not eliminate these matches, which will result in secondary auto-correlation peaks. In size, the blade edges will match over a wide range of sizes, although the radial edges of the holes will not.

In summary the basfan is good on all criteria of speed, accuracy, and yield, but there is still room for improvement.

- 1 Figure 14 illustrates the next refinement. The radial features of previous fan configurations cause
- both grid degeneracy and self-similarity in size. A simple change to the formulas defining the fan
- 3 in polar coordinates allows us to generate radial features that are sections of spiral curves,
- 4 resulting in shape 1400. This is the first of two steps leading towards our final fan configuration,
- 5 the balanced radically asymmetric fan (bradfan).
- 6 In polar coordinates, the bradfan after the first modification 1450 can be compared with the
- 7 basfan 1350. Considering a particular blade 1404, the dotted lines show the blade edges before the
- 8 change (basfan), and the solid lines show the blade and hole for bradfan 1400, 1450. As can be
- 9 seen, the outer edge of the blade has not moved, but where the blade connects with the hub has
- been moved by an amount 1406 called skew.
 - The blade parameters for the bradfan so far are given in table 12.

Table 12. Bradfan parameters, step 1				
Blade	Starting Azimuth	Width	Skew	
1410, 1460	0°	38°	11°	
1420, 1470	57°	50°	-11°	
1430, 1480	146°	74°	-22°	
1440, 1490	269°	62°	22°	

This simple change eliminates all straight radial features in the final rendering, which eliminates grid degeneracy and size self-similarity. The skew parameters are chosen to be different for each blade, so that blade edges will not match those of other blades under rotation. This reduces some, but not most, of the rotation self-similarity. All figures of merit improve over basfan, as can be seen in table 13.

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Table 13. Bradfan step 1				
R S worst $T(\theta)$ best $T(\theta)$ GD				
$5.88 r^2$ $5.71 r^2$ $8.82 r @ 37^\circ$ $9.51 r @ 137^\circ$ 0				0

- Figure 15 illustrates the second and final step in making the bradfan, which eliminates the final
- 2 rotation self-similarity. This is done by making the outer blade edges also spiral sections, instead
- 3 of circular. The final bradfan 1500 is shown, also drawn in polar coordinates 1550. A particular
- 4 bradfan blade 1504 in polar coordinates shows both the skew parameter 1506 and a new spiral
- 5 parameter 1508. The complete blade parameters are given in table 14, and the final figures of
- 6 merit in table 15.
 - Unlike previous fan parameters, which were chosen by hand, these parameters were obtained by an automated search of the 41,472 distinct arrangements of the 16 blade parameters, followed by a manual examination of the 100 highest ranking permutations.

Table 14. Final bradfan blade parameters				
Blade	Starting Azimuth	Width	Skew	Spiral
1510, 1560	0°	62°	22°	0.09 r
1520, 1570	81°	74°	-11°	0.03 r
1530, 1580	184°	50°	-22°	-0.09 r
1540, 1590	283°	38°	11°	-0.03 r

- 11 The hub, hole, and rounding parameters are as before. Note that the spiral parameters are
- 12 different for each blade to avoid rotation self-similarity.

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Table 15. Final bradfan					
R	S	worst $T(\theta)$	best $T(\theta)$	GD	
$6.12 r^2$	$6.12 r^2$	9.06 r @ 137°	9.50 r @ 68°	0	

- 1 The worst case translation figure of merit is over 9 r, which is 225% better than the worst case
- 2 for a cross, and translation is well balanced over all angles. The automated search has given us
- 3 superb and perfectly balanced R and S values. R is 53% better than a cross or square at the same
- 4 radius, and S is just about what a complete circle would be.
- 5 The bradfan has no fine features and so should be fast to find and survive most manufacturing
- 6 processes well. It has excellent figures of merit in all degrees of freedom and no grid degeneracy.
- It has no significant self-similarities in any degree of freedom, and looks nothing like any shape in common use. The bradfan is an ideal universal alignment target.

Figure 16 illustrates an apparatus for locating objects using cooperative targets. An object 1600 is located somewhere in space relative to some object or device intended to grip, operate on, dock with, avoid, or otherwise interact with the object 1600, such as the illustrated robot gripper 1660. The object 1600 contains a cooperative target 1610. A camera or other suitable image forming device 1620 is located in a known position and attitude in space relative to the gripper 1660, and such that the cooperative target 1610 appears in the field of view of the camera 1620.

The object's location relative to the gripper 1660 and camera 1620 may be uncertain in various degrees of freedom, including translation degrees of freedom 1680 and 1682, orientation degree of freedom 1684, and distance degree of freedom 1686.

The camera 1620 is connected to a machine vision system 1630, which produces as part of its operation, using means well-known in the art, a digital image 1635. The digital image 1635 will contain an image of the cooperative target 1610. The location of the target in the image will be uncertain is various degrees of freedom, such as translation, orientation, and size, that correspond to the uncertainties in location of the object 1600 in space, for example 1680, 1682, 1684, and 1686, where said correspondence is described by well-known mathematical formulas.

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- 1 The machine vision system 1630 contains an alignment algorithm 1640 that reads and analyzes the
- 2 digital image 1635 to determine the location of the target in the digital image. Using this
- 3 information the machine vision system 1630 computes the location in space of the target 1610
- 4 using well-known formulas, and communicates this information to some device, such as robot
- 5 controller 1650, for use in gripping, operating on, docking with, avoiding, or otherwise interacting
- 6 with the object 1600.
- 7 In one embodiment of the invention, the alignment algorithm 1640 is capable of aligning non-
- 8 translation degrees of freedom such as orientation and size, and the cooperative target 1610
- 9 conveys sufficient information in such degrees of freedom to enable the alignment algorithm
- 10 1640 to make such measurements. In another embodiment of the invention, targets are used that
- 11 have at least one of the following attributes:
 - They satisfy the invention's evaluation criteria.
 - They result from the use of the invention's design method.
 - They have no significant rotational symmetry
 - They have no significant orientation or size self-similarity
 - They are not primarily composed of circles, circular arcs, straight lines, or right angles.

In a preferred embodiment, a universal alignment target such as 1500 is used in conjunction with an alignment algorithm 1640 capable of aligning non-translation degrees of freedom, such as one of the many products available today offering such capabilities.

Other modifications and implementations will occur to those skilled in the art without departing from the spirit and the scope of the invention as claimed. Accordingly, the above description is not intended to limit the invention except as indicated in the following claims.

What is claimed is:

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- 1 1. A method for locating an object, the method comprising:
- 2 Rendering an alignment target on the object, the alignment target being adapted to be
- 3 substantially rotationally asymmetric and substantially size self-dissimilar; and
- 4 Searching for the alignment target so as to provide the pose of the object.

A method and apparatus for locating objects by means of machine vision alignment using cooperative targets. Novel cooperative targets are used that have substantial performance advantages. Alignment methods having non-translation alignment capabilities are used, such as geometric pattern matching, cooperating with suitable targets to perform alignment in non-translation degrees of freedom, such as orientation and size.

ABSTRACT

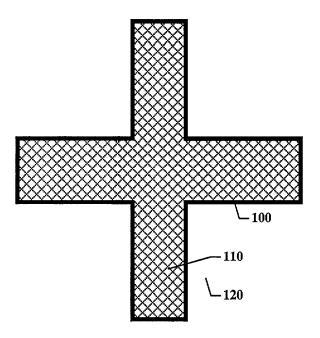


Figure 1—A common cooperative target

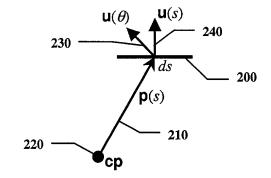


Figure 2. Element of figure of merit

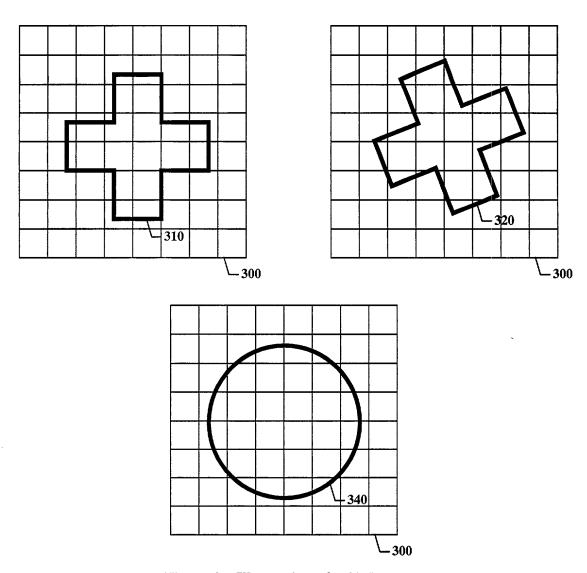


Figure 3—Illustration of grid degeneracy

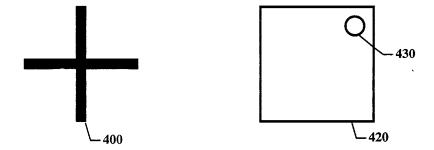


Figure 4—Illustration of speed criteria

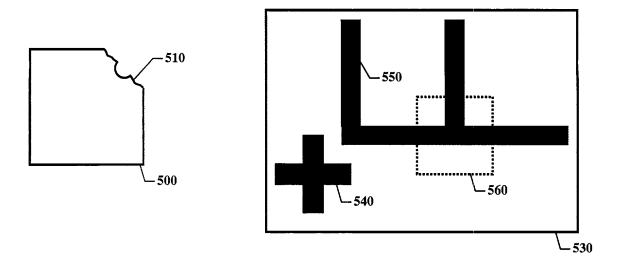


Figure 5—Illustration of yield criteria

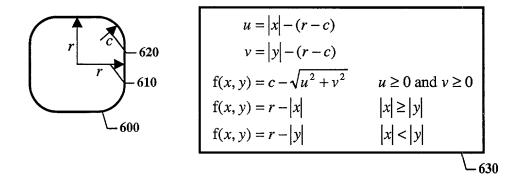


Figure 6—Targets defined algebraically are easy to use

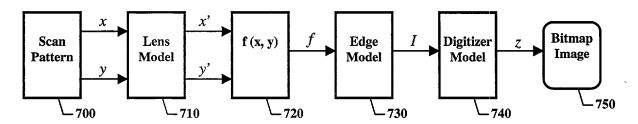


Figure7—Target rendering method

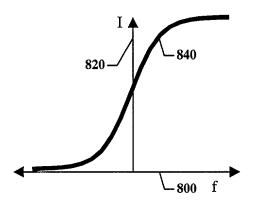


Figure 8—Intensity profile function used in target rendering method

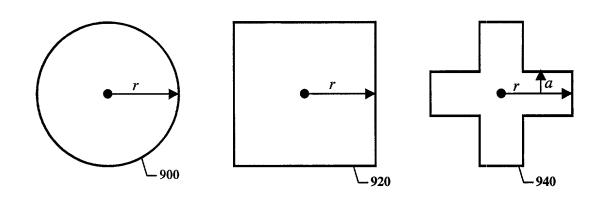


Figure 9—Common alignment targets

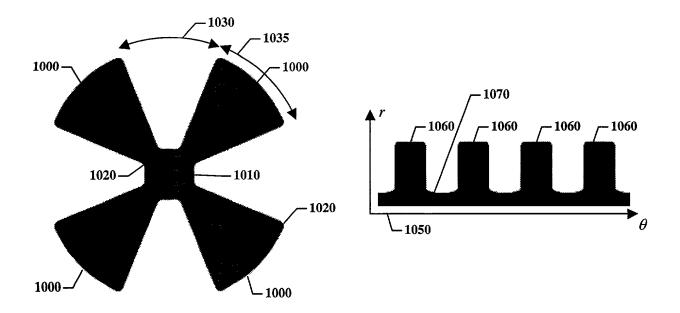


Figure 10—Primitive fan

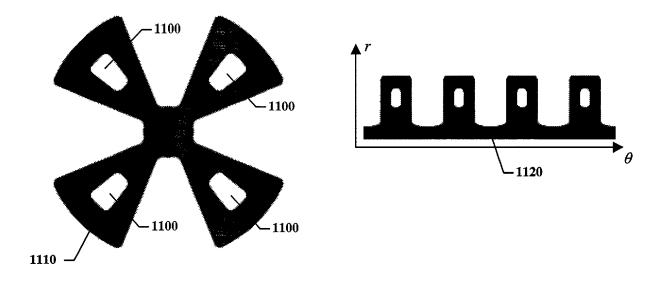


Figure 11—Simple fan

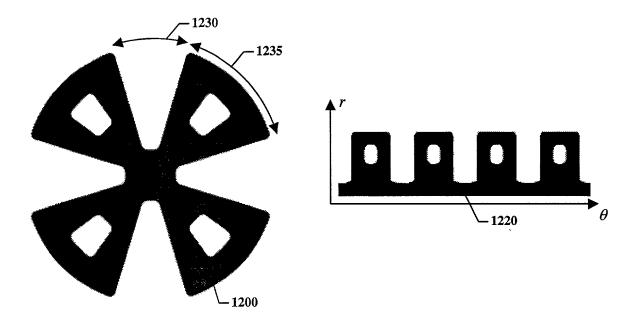


Figure 12—Balanced fan

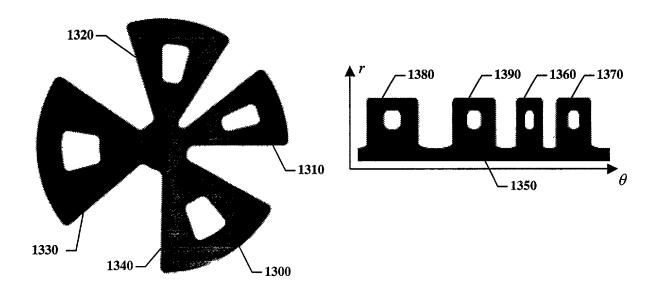


Figure 13—Balanced asymmetric fan

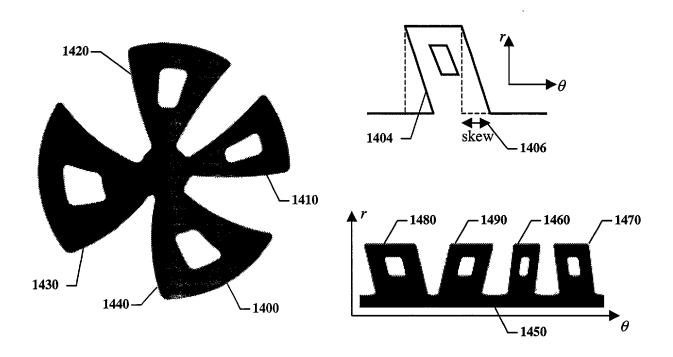


Figure 14—Balanced radically asymmetric fan, step 1

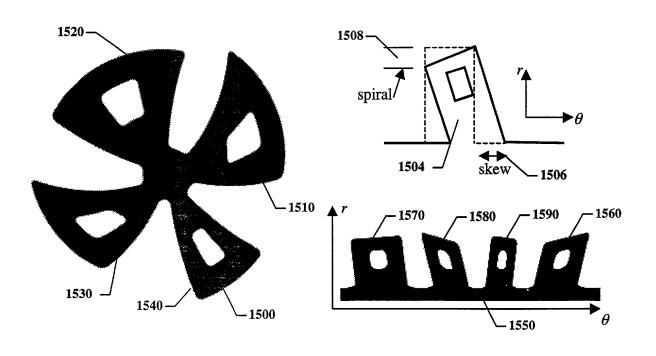


Figure 15—Balanced radically asymmetric fan (UAT)

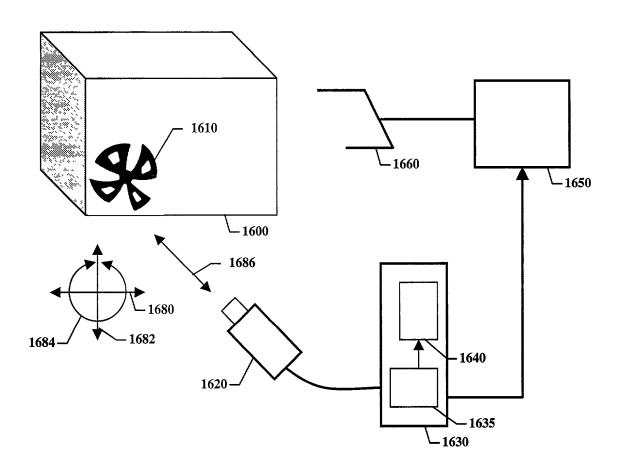


Figure 16—Apparatus for locating objects using a UAT

IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

APPENDIX FOR PATENT APPLICATION

of

William Silver

for

METHOD AND APPARATUS FOR LOCATING OBJECTS USING UNIVERSAL ALIGNMENT TARGETS

Attorney Docket Number: C00-057

Express Mail Certificate Number: EM 067 610 794 US

Attribute VB_Name = "shapes"

```
img.Pixel(i, j) = rp.pixelValue(shape.profileCoord(i - x0, y0 - j))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Public Sub scanContours(shape As Object, step As Double, points As ContourSet)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Public Sub render(shape As Object, img As Bmp, rp As RenderProfile) Dim i As Integer, j As Integer
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              For i = 0 To img.width - 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Dim x0 As Double, y0 As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ' radians
                                                                                                                                                                                                                                                                                                                                                                                                                                              centerOfProjectionX As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       centerOfProjectionY As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 translationMerit(1) As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         translationAngle(1) As Double
                                                                                                                                                                                                                                                                                      segments() As ContourSegment
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              y0 = img.Height / 2 - 0.5
For j = 0 To img.Height - 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        x0 = img.width / 2 + 0.5
                                                 Public Type ContourSegment
                                                                                                                                                                                                                                                                                                                                                                                         lists() As ContourList
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       angleMerit As Double
                                                                                                                                                                                                                                                                                                                                                                                                                    perimeter As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                sizeMerit As Double
                                                                                                                                                                                                                                                           Public Type ContourList
                                                                                                                                                                                                                                                                                                                                                               Public Type ContourSet
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Const gate ≈ 0.1
                                                                                                                            len As Double
                                                                                                                                                      udx As Double
                                                                                                                                                                             udy As Double
                                                                        x As Double
                                                                                                 y As Double
Option Explicit
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Next i
                                                                                                                                                                                                          End Type
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           End Sub
```

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Const maxSteps = 100000

Const block = 100

```
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```

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```
If gt <= -pi Then Err.Raise vbObjectError + 200, , "Lost contour CW at (" & Format(x, "0.00") & ") after " & si & " steps"
                                                      px = px - u * dx
py = py - u * dy
If Sqr(px ^ 2 + py ^ 2) <= step / 2 Then
                                                                                                                                                                                                                                                                             sn = Sin(gt)
xn = x + step * (dx * cs - dy * sn)
yn = y + step * (dx * sn + dy * cs)
an = shape.profileCoord(xn, yn)
                                                                                           "," & Format(y, "0.00") & ") after " & si & " steps"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ' get next point, distance, direction
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            xp = xp + (xn - xp) * ap / (ap - an)

yp = yp + (yn - yp) * ap / (ap - an)

r = Sqr((xp - x) ^ 2 + (yp - y) ^ 2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                If 0 < u And u <= 1.01 * r Then
                                                                                                                                                                                                                                                                                                                                                            If an < 0 Then Exit Do
                                                                                                                                                                                               gt = gt - gate
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            u = px * dx + py * dy
                                                                                                                                                                                                                                                          cs = Cos(gt)
                                                                                                                                                                                                                                                                                                                                                                                                                                            pn = pn + 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         dx = (xp - x) / rdy = (yp - y) / r
                                                                                                                                                                             Do While True
                                                                                                                pn = pn + 1
                                                                                                                                                                                                                                                                                                                                                                                  ux = dx
                                                                                                                                                                                                                                                                                                                                                                                                      yp = yn
                                                                                                                                                                                                                                                                                                                                                                                                                         ap = an
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    , test for done
                                                                                                                                                       If an = 0 Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     px = x0 - x
py = y0 - y
xn = xp

yn = yp

an = ap
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Loop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 End If
                                                                                                                                       Loop
```

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```
ReDim Preserve points.lists(ci).segments(si - 1 + block)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Err.Raise vbObjectError + 201, , "Can't find end of contour"
                                                                                                                                                                                       If si > UBound(points.lists(ci).segments) Then
                                   r = Sqr((xp - x) ^2 + (yp - y) ^2 )

dx = (xp - x) / r

dy = (yp - y) / r

done = True
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ReDim Preserve points.lists(ci).segments(si - 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Public Sub computeMerit(contours As ContourSet)
                                                                                                                                                                                                                                                                  With points.lists(ci).segments(si)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         If Not done Then ' logic error in algorithm
                                                                                                                                                                                                                                                                                                                                                                                                                                        perimeter = perimeter + r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            points.perimeter = perimeter
pn = pn + 2 * si + 2
                                                                                                                                                                      ' write next point
xp = x0
yp = y0
                                                                                                                                                                                                                                                                                                                                                                                                                     ' update stats
                                                                                                                                                                                                                                                                                                                                          xp = xp\dot{n}
                                                                                                                                                                                                                                                                                                                                                                .udy = dy
                                                                                                                                                                                                                                                                                                                           .len = r
                                                                                                            End If
End If
                                                                                                                                                                                                                                                                                                                                                                                                                                                           si = si + 1
                                                                                                                                                                                                                                                                                       × :
                                                                                                                                                                                                                                                                                                         \cdot Y = Y
                                                                                                                                                                                                                                                                                                                                                                                End With
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  y = yp
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 dx = x
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    End If
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Next ci
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                End Sub
```

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```
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```

Dim ci As Long, si As Long, d As Integer

```
Dim x As Double, y As Double, r As Double, t As Double, cs As Double, sn As Double
                                       Dim Src As Double, Srs As Double, Ss2 As Double, Sc2 As Double, Scs As Double
                                                                                                                                                                                                                                                                                                                                                                                                                             r = (.x + .udx * .len / 2) * cs + (.y + .udy * .len / 2) * sn
                                                                                                                 Dim Strans(179) As Double, csTab(179) As Double, snTab(179) As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              x = .x + .udx * .len / 2 - contours.centerOfProjectionX y = .y + .udy * .len / 2 - contours.centerOfProjectionY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Scross = Scross + .len * Abs(x * .udx + y * .udy)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  contours.centerOfProjectionY = (Srs * Sc2 - Src * Scs) / r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  contours.centerOfProjectionX = (Src * Ss2 - Srs * Scs) / r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Sdot = Sdot + .len * Abs(x * .udy - y * .udx)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    For si = 0 To UBound(contours.lists(ci).segments)
                                                                                                                                                                                                                                                                    For si = 0 To UBound(contours.lists(ci).segments)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            With contours.lists(ci).segments(si)
                                                                                                                                                                                                                                                                                                              With contours.lists(ci).segments(si)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Srs = Srs + .len * r * sn
Ss2 = Ss2 + .len * sn * sn
Sc2 = Sc2 + .len * cs * cs
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Scs = Scs + .len * cs * sn
                                                                                                                                                                                                                                                                                                                                                                                                                                                               Src = Src + .len * r * cs
                                                                            Dim Sdot As Double, Scross As Double
                                                                                                                                                                                                                                  For ci = 0 To UBound(contours.lists)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             For ci = 0 To UBound (contours.lists)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ' compute sine and cosine tables For d\,=\,0 To 179
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ' angle and size
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              r = Sc2 * Ss2 - Scs ^ 2
                                                                                                                                                                                                                                                                                                                                                                                             sn = -.udx
                                                                                                                                                                                               ' center of projection
                                                                                                                                                                                                                                                                                                                                                     cs = .udy
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  csTab(d) = Cos(t)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          snTab(d) = Sin(t)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        t = d * degToRad
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ' figures of merit
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               End With
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Next si
```

```
Strans(d) = Strans(d) + .len * Abs(csTab(d) * .udy - snTab(d) * .udx)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                x1 = cs.lists(ci).segments(UBound(cs.lists(ci).segments)).x
y1 = cs.lists(ci).segments(UBound(cs.lists(ci).segments)).y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ElseIf Strans(d) > contours.translationMerit(1) Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Public Sub drawContours(cs As ContourSet, dsply As Display)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              If Strans(d) < contours.translationMerit(0) Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             tblt.DrawLine x1, y1, .x, .y, vbGreen
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               contours.translationMerit(0) = Strans(d)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           contours.translationMerit(1) = Strans(d)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               For si = 0 To UBound(cs.lists(ci).segments)
                                                                                                                                                                                                                                                                                                                                                                         contours.translationMerit(d) = Strans(0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     contours.translationAngle(1) = d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             contours.translationAngle(0) = d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           With cs.lists(ci).segments(si)
                                                                                                                                                                                                                                                                                                                                                                                                      contours.translationAngle(d)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Dim x1 As Double, y1 As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    For ci = 0 To UBound(cs.lists)
                                                                                                                                                                                                                                                                                                             ' translation figures of merit
                         For d = 0 To 179
                                                                                                                                                                                                                  contours.angleMerit = Scross
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Dim ci As Long, si As Long
' translation
                                                                                                                                                                                                                                                  contours.sizeMerit = Sdot
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Dim tblt As New tablet
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      y1 = .y
End With
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           x1 = .x
                                                                                         Next d
                                                                                                                       End With
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    For d = 1 To 179
                                                                                                                                                                                                                                                                                                                                         For d = 0 To 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        End If
                                                                                                                                                                                                                                                                                                                                                                                                                                          Next d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Next d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  End Sub
```

SCANNED, # /×

```
Public Function rmod(x As Double, m As Double) As Double
dsply.DrawSketch tblt, ClientCoordinates
End Sub
                                                                                                                                                                                                                                                                                                                                                                                                      atan2 = 1.5 * pi + Atn(x / -y)
                                                                                                                                                                                                                                                                                                                          atan2 = halfpi - Atn(x / y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     atan2 = twopi + Atn(y'/x)
                                                                                                             Public Const pi = 3.14159265358979

Public Const twopi = 2 * pi

Public Const halfpi = pi / 2

Public Const degToRad = twopi / 360
                                                                                                                                                                                                                                                                                                                                                                                                                                                      atan2 = Atn(y / x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rmod = x - Int(x / m) * m
                                                                Attribute VB_Name = "vbMath"
                                                                                                                                                                                                                                                                                                                                                                                                                     ElseIf y >= 0 Then
                                                                                                                                                                                                                                                                                                                                                                        If -y > x Then
' 225 - 315
                                                                                                                                                                                                                                                                                                          , 45 - 135
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    , 315 - 0
                                                                                                                                                                                                                                                                                                                                                                                                                                     , 0 - 45
                                                                                                                                                                                                                                                                                                                                         End If
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      End If
                                                                               Option Explicit
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   End Function
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     End Function
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     End If
```

SCANNED, # /S

Next si

Next ci

```
Public Function limit(x As Variant, lo As Variant, hi As Variant) As Variant
                                                                                                                 Public Function splitmod(lo As Double, hi As Double, m As Double) As Double
                                                                                                                                                                                                                                                                                                                                                Public Function max(a As Variant, b As Variant) As Variant
If a > b Then max = a Else max = b
                                                                                                                                                                                                                                 Public Function min(a As Variant, b As Variant) As Variant
Public Function smod(x As Double, m As Double) As Double smod = rmod(x + m / 2, m) - m / 2
                                                                                                                                           splitmod = rmod(lo + smod(hi - lo, m) / 2, m)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           'NotAnMTSObject
                                                                                                                                                                                                                                                         If a < b Then min = a Else min = b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Attribute VB_GlobalNameSpace = False
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Attribute VB_Name = "RenderProfile"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Persistable = 0 'NotPersistable
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DataBindingBehavior = 0 'vbNone
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Attribute VB_PredeclaredId = False
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              'vbNone
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Attribute VB_Creatable = True
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Attribute VB_Exposed = False
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MTSTransactionMode = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DataSourceBehavior = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ElseIf x >= hi Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        MultiUse = -1 'True
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               If x \leftarrow 10 Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        limit = lo
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              limit = hi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     limit = x
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                VERSION 1.0 CLASS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Option Explicit
                                                                                                                                                                                                                                                                                                                                                                                                          End Function
                                                                                                                                                                                                                                                                                        End Function
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   End Function
                                                                                                                                                                         End Function
                                                         End Function
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       End If
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Else
```

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```
realIntensity = background + (Sgn(profileCoord) + 1) / 2 * contrast
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          realIntensity = background + contrast / (1# + Exp(-a))
                                                                                                                                           Public Function realIntensity(profileCoord As Double) As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Public Function pixelValue(profileCoord As Double) As Byte
                                                                                                                                                                                                                                                                                                                                                                                                                                realIntensity = background + contrast
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   'NotAnMTSObject
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         z = realIntensity(profileCoord) + 0.5
                                                                                                                                                                                                                                                                                                                                                                          realIntensity = background
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Attribute VB_GlobalNameSpace = False
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Persistable = 0 'NotPersistable
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          DataBindingBehavior = 0 'vbNone
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        'vbNone
                                                                                                                                                                                                                                                                                                                  a = profileCoord / sigmoid
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Attribute VB_Name = "FanShape"
                                                                                                                                                                                                                                                                                                                                                                                                    ElseIf a >= 20 Then
                           Public background As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                If z > 255 Then z = 255
                                                        Public contrast As Double
Public sigmoid As Double
                                                                                                                                                                                                                                                                                                                                             If a <= -20 Then
                                                                                                                                                                                                                             If sigmoid = 0 Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      If z < 0 Then z = 0
                                                                                    Public noise As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  MultiUse = -1 'True
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   MTSTransactionMode
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DataSourceBehavior
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Dim z As Double
                                                                                                                                                                      Dim a As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               pixelValue = z
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            VERSION 1.0 CLASS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      End If
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           End Function
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              End Function
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   End If
```

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Const bladeNum = 4

center to edge radius difference, fraction of outer radius azimuth difference, outer to origin, degrees start of blade at outer radius, degrees width of blade, degrees Private Type BladeParams azimuth As Double spiral As Double width As Double skew As Double End Type

blades(bladeNum - 1) As BladeParams holeThickness As Double holeInnerRad As Double holeOuterRad As Double innerRad As Double outerRad As Double Private Type FanParams round As Double End Type

holeInnerRound As Double holeOuterRound As Double bladeRound As Double halfWidth As Double holeZoneT As Double zoneWidth As Double widthSkew As Double hubRound As Double holeRadT As Double Private Type BladeData lowSkew As Double zoneLow As Double center As Double spiral As Double skew As Double high As Double low As Double

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End Type

```
.spiral = fp.blades(k).spiral / .halfWidth * outerRad
.holeRadT = fp.holeThickness * .halfWidth
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           holeZoneRHigh = (.holeOuterRad + 1) / 2 * outerRad
holeCenterR = (.holeInnerRad + .holeOuterRad) / 2 * outerRad
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 .center = rmod(.low * degToRad + .halfWidth, twopi)
.skew = .skew / outerRad * degToRad
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      holeRadR = (.holeOuterRad - .holeInnerRad) / 2 * outerRad
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               .halfWidth = fp.blades(k).width * degToRad / 2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    .holeZoneT = (.holeRadT + .halfWidth) / 2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Dim k As Integer, knext As Integer, kprev As Integer
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      holeZoneRLow = .holeInnerRad / 2 * outerRad
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    .low = fp.blades(k).azimuth - .skew
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         .high = fp.blades(k).width + .low
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            .skew = fp.blades(k).skew
                                                                                                                                                                                           Private blades(bladeNum - 1) As BladeData
                                                                                                                                                                                                                                                                                                                                                                                                                              Private Sub loadFanData(fp As FanParams)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           innerRad = .innerRad * outerRad
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            If .holeRadT > 0 Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 For k = 0 To bladeNum - 1
                                  Private paramsChanged As Boolean
                                                                                                                                                                                                                                                                     Private holeZoneRHigh As Double
                                                                                                                                                                                                                                  Private holeZoneRLow As Double
                                                                                                                                                                                                                                                                                                             Private holeCenterR As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        outerRad = .outerRad
Private params As FanParams
                                                                                                                                                   Private innerRad As Double
                                                                                                                                                                                                                                                                                                                                                Private holeRadR As Double
                                                                                                                Private outerRad As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           With blades(k)
```

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.bladeRound = min(fp.round, min((outerRad - innerRad) / 2, .halfWidth * outerRad))

.holeZoneT = 0

```
innerRad * .skew) - (blades(kprev).center + blades(kprev).halfWidth + innerRad * blades(kprev).skew), twopi), 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                               .hubRound = min(fp.round, min((outerRad - innerRad) / 2, max(smod((.center - .halfWidth +
                                                                                                                                                                                                                                                                                                                                                      .lowSkew = (.skew + blades(kprev).skew) / 2
.zoneWidth = rmod(splitmod(.high, blades(knext).low, 360) * degToRad - .zoneLow, twopi)
.holeInnerRound = min(fp.round, min(holeRadR, .holeRadT * fp.holeInnerRad * outerRad)) .holeOuterRound = min(fp.round, min(holeRadR, .holeRadT * fp.holeOuterRad * outerRad))
                                                                                                                                                                                                                                                                                                                      .zoneLow = splitmod(blades(kprev).high, .low, 360) * degToRad
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Dim r As Double, t As Double, u As Double, v As Double, round As Double
                                                                                                                                                                                                                                                                                                                                                                                                                             .widthSkew = (.skew + blades(knext).skew) / 2 - .lowSkew
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Public Function profileCoord(x As Double, y As Double) As Double
                                                                                                                                                                                                                                        knext = (k + 1) Mod bladeNum kprev = (k - 1 + bladeNum) Mod bladeNum
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Dim rh As Double, rp As Double, a As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ' figure out which blade to make
For k = 0 To bladeNum - 1
With blades(k)
                                                                                                                                                                           For k = 0 To bladeNum - 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 paramsChanged = False
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             loadFanData params
                                                                                                                                                                                                             With blades(k)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            r = Sqr(x^2 + y^2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        If paramsChanged Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Private Sub getFanData()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Dim k As Integer
                                                                    End With
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           End With
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               t = atan2(y, x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Enc
Next k
End With
End Sub
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 * innerRad / 2))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        getFanData
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 End If
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      End Sub
```

```
If rmod(t - (.zoneLow + r * .lowSkew), twopi) < .zoneWidth + r * .widthSkew Then Exit For
                                                                                  If k = bladeNum Then Err.Raise vbObjectError + 100, , "Bad blade detection logic"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               If holeZoneRLow < rp And rp < holeZoneRHigh And t < .holeZoneT Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ElseIf rh - holeRadR >= r * (t - .holeRadT) Then
                                                                                                                                                                                                                                                                                                                       round = blades((k + 1) Mod bladeNum).hubRound
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          v = r * t - (r * .halfWidth - .bladeRound)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ' "<" instead of "<=" so hole can be disabled
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      a = .bladeRound - Sgr(u^2 + v^2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ' determine zone and distance from edge
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       v = r * t - (r * .holeRadT - round)
If u > 0 And v > 0 Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 a = Sqr(u^2 + v^2) - round
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              u = rp - (outerRad - .bladeRound)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 round = .holeOuterRound
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      round = .holeInnerRound
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           a = r * (t - .holeRadT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              u = rh - (holeRadR - round)
                                                                                                                                                                         ' get blade relative azimuth
                                                                                                                                                                                                                               t = smod(t - .center, twopi)
rp = r - t * .spiral
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          If u > 0 And v > 0 Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rh = rp - holeCenterR
If rh >= 0 Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               a = rh - holeRadR
                                                                                                                                                                                                                                                                                                                                                                                                              round = .hubRound
                                                                                                                                                                                                   t = t - r * .skew
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rh = -rh
                                                                                                                                                                                                                                                                                         If t >= 0 Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     End If
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    End If
                                                                                                                                                                                                                                                                                                                                                                                  t = -t
                                                                                                                                            With blades(k)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Else
                            End With
                                                                                                                                                                                                                                                                                                                                                                                                                                          End If
```

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Else

```
img.Pixel(i, j) = rp.pixelValue(profileCoord(i - x0, y0 - j))
                                                                                                ElseIf rp - outerRad >= r * (t - .halfWidth) Then
                                                                                                                                                   ElseIf r - innerRad >= r * (t - ,halfWidth) Then
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Public Property Let outerRadius(ByVal vNewValue As Double)
                   v = r * t - (r * .halfWidth + round)
                                                                        a = Sqr(u^2 + v^2) - round
                                                                                                                                                                                                                                                                                                                                                                                                                                                                Public Sub render(img As Bmp, rp As RenderProfile)
                                                                                                                                                                             a = r * (.halfWidth - t)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Public Property Get outerRadius() As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Public Property Get numBlades() As Variant
u = r - (innerRad + round)
                                               If u < 0 And v < 0 Then
                                                                                                                           a = outerRad - rp
                                                                                                                                                                                                                               a = innerRad - r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Dim i As Integer, j As Integer
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Dim x0 As Double, y0 As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         For i = 0 To img.width - 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                outerRadius = params.outerRad
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  x0 = img.width / 2 + 0.5
y0 = img.Height / 2 - 0.5
For j = 0 To img.Height - 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             numBlades = bladeNum
                                                                                                                                                                                                                                                       End If
                                                                                                                                                                                                      Else
                                                                                                                                                                                                                                                                                                                                                                                    profileCoord = a
                                                                                                                                                                                                                                                                              End If
End If
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Next i
                                                                                                                                                                                                                                                                                                                                                                                                                End Function
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          End Property
                                                                                                                                                                                                                                                                                                                                    End With
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    End Property
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Next j
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                End Sub
```

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```
Attribute innerRadius.VB_Description = "Radius of fan hub, fraction of outer radius"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Attribute cornerRound.VB_Description = "Corner radius, absolute units"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Public Property Let azimuth(bn As Integer, ByVal vNewValue As Double)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Attribute azimuth.VB_Description = "Azimuth of blade bn in degrees"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Public Property Let width(bn As Integer, ByVal vNewValue As Double)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Attribute width.VB_Description = "Width of blade bn in degrees"
                                                                                                                                                                                                                                                                                                                                                                Public Property Let innerRadius(ByVal vNewValue As Double)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Public Property Let cornerRound(ByVal vNewValue As Double)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            params.blades(bn).width = limit(vNewValue, 0, 360)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Public Property Get azimuth(bn As Integer) As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               params.blades(bn).azimuth = rmod(vNewValue, 360)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Public Property Get width(bn As Integer) As Double
                                                                                                                                                                                                                                                                                                                                                                                                     params.innerRad = limit(vNewValue, 0, 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Public Property Get cornerRound() As Double
                                                                                                                                                            Public Property Get innerRadius() As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  azimuth = params.blades(bn).azimuth
params.outerRad = max(vNewValue, 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    params.round = max(vNewValue, 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               width = params.blades(bn).width
                                                                                                                                                                                                                                           innerRadius = params.innerRad
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cornerRound = params.round
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           paramsChanged = True
                                       paramsChanged = True
                                                                                                                                                                                                                                                                                                                                                                                                                                                 paramsChanged = True
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 paramsChanged = True
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                End Property
                                                                              End Property
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      End Property
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      End Property
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         End Property
                                                                                                                                                                                                                                                                                  End Property
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               End Property
```

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```
Attribute skew.VB_Description = "Blade skew (hub to circumference offset) in degrees"
SCANNED, # /
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Attribute spiral.VB_Description = "Outer blade edge radial difference"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Public Property Let spiral(bn As Integer, ByVal vNewValue As Double)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Public Property Let skew(bn As Integer, ByVal vNewValue As Double)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       params.blades(bn).spiral = limit(vNewValue, -0.5, 0.5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      params.blades(bn).skew = limit(vNewValue, -90, 90)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Public Property Get spiral(bn As Integer) As Double
                                                                                                                                                                                                                                                                             Public Property Get skew(bn As Integer) As Double
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      spiral = params.blades(bn).spiral
                                                                                                                                                                                                                                                                                                                                                      skew = params.blades(bn).skew
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               paramsChanged = True
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             paramsChanged = True
                                                                                                                                                                 paramsChanged = True
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          End Property
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               End Property
                                                                                                                                                                                                     End Property
                                                                                                                                                                                                                                                                                                                                                                                          End Property
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 End Property
```

```
Public Property Let holeInnerRadius(ByVal vNewValue As Double)
                                                                                                                                              params.holeInnerRad = limit(vNewValue, 0, 1)
                                                                                                                                                                                                                                                                                                 Public Property Get holeOuterRadius() As Double
holeInnerRadius = params.holeInnerRad
                                                                                                                                                                                    paramsChanged = True
                                                                                                                                                                                                                        End Property
                                      End Property
```

Attribute holeInnerRadius.VB_Description = "Fraction of outerRadius"

Public Property Get holeInnerRadius() As Double

Attribute holeOuterRadius.VB_Description = "Fraction of outerRadius"

holeOuterRadius = params.holeOuterRad

End Property

Public Property Let holeOuterRadius(ByVal vNewValue As Double) params.holeOuterRad = limit(vNewValue, 0, 1) paramsChanged = True rrinted 10/29/99

Printed 10/29/99

Private Sub Class_Initialize()

Dim i As Integer

t = blades(k).center + r * blades(k).skew

x = r * Cos(t) y = r * Sin(t)End Sub

r = holeCenterR + holeRadRk = i - 1

End Select

Case 1 To 4

r = outerRadk = 0

Select Case i

Case 0

```
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```

```
End Property
```

```
Public Property Get holeWidth() As Double Attribute holeWidth.VB_Description = "Width of holes, fraction of blade widths"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Public Sub getContourStart(i As Integer, x As Double, y As Double)
                                                                                                                                                                 Public Property Let holeWidth(ByVal vNewValue As Double)
                                                                                                                                                                                                 params.holeThickness = limit(vNewValue, 0, 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Dim r As Double, t As Double, k As Integer
                                                                                                                                                                                                                                                                                                                              Public Property Get numContours() As Integer
                                                                   holeWidth = params.holeThickness
                                                                                                                                                                                                                                                                                                                                                                If params.holeThickness > 0 Then
                                                                                                                                                                                                                                  paramsChanged = True
                                                                                                                                                                                                                                                                                                                                                                                               numContours = 5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   numContours = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           getFanData
                                                                                                                                                                                                                                                               End Property
                                                                                                  End Property
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  End Property
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                End If
```

```
.holeThickness = 0.33

For i = 0 To bladeNum - 1

With .blades(i)

.azimuth = (i + 0.25) * 360 / bladeNum

.width = 360# / (2 * bladeNum)
                                                                                                                                                                                .skew = 0
.spiral = 0
End With
                                                             .holeInnerRad = 0.5
.holeOuterRad = 0.8
                                                                                                                                                                                                                                                               paramsChanged = True
End Sub
               .outerRad = 128
.innerRad = 0.2
                                                .round = 6
With params
                                                                                                                                                                                                                                Next i
End With
```

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